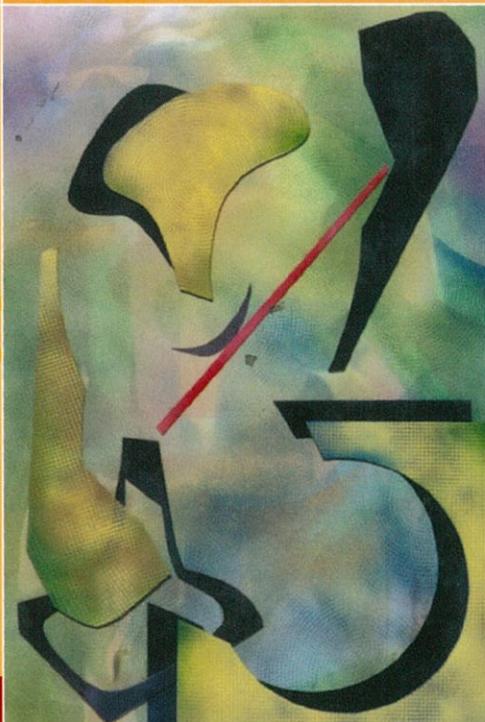


Zbigniew Michalewicz
David B. Fogel

How to Solve It: Modern Heuristics

Second Edition



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Table of Contents

Introduction	1
I What Are the Ages of My Three Sons?	9
1 Why Are Some Problems Difficult to Solve?	11
1.1 The size of the search space	11
1.2 Modeling the problem	16
1.3 Change over time	19
1.4 Constraints	21
1.5 The problem of proving things	24
1.6 Your chance for glory	26
1.7 Summary	29
II How Important Is a Model?	31
2 Basic Concepts	35
2.1 Representation	35
2.2 The objective	36
2.3 The evaluation function	37
2.4 Defining a search problem	39
2.5 Neighborhoods and local optima	40
2.6 Hill-climbing methods	43
2.7 Can you sink this trick shot?	45
2.8 Summary	48
III What Are the Prices in 7–11?	49
3 Traditional Methods — Part 1	55
3.1 Exhaustive search	58
3.1.1 Enumerating the SAT	59
3.1.2 Enumerating the TSP	61
3.1.3 Enumerating the NLP	62
3.2 Local search	64
3.2.1 Local search and the SAT	65
3.2.2 Local search and the TSP	66

3.2.3	Local search and the NLP	69
3.3	Linear programming: The simplex method	76
3.4	Summary	80
IV	What Are the Numbers?	83
4	Traditional Methods — Part 2	87
4.1	Greedy algorithms	87
4.1.1	Greedy algorithms and the SAT	87
4.1.2	Greedy algorithms and the TSP	89
4.1.3	Greedy algorithms and the NLP	90
4.2	Divide and conquer	90
4.3	Dynamic programming	93
4.4	Branch and bound	101
4.5	A^* algorithm	105
4.6	Summary	109
V	What's the Color of the Bear?	111
5	Escaping Local Optima	115
5.1	Simulated annealing	117
5.2	Tabu search	125
5.3	Summary	134
VI	How Good Is Your Intuition?	135
6	An Evolutionary Approach	139
6.1	Evolutionary approach for the SAT	142
6.2	Evolutionary approach for the TSP	145
6.3	Evolutionary approach for the NLP	149
6.4	Summary	151
VII	One of These Things Is Not Like the Others	157
7	Designing Evolutionary Algorithms	161
7.1	Representation	165
7.1.1	Fixed-length vectors of symbols	166
7.1.2	Permutations	167
7.1.3	Finite state machines	168
7.1.4	Symbolic expressions	168
7.2	Evaluation function	169
7.3	Variation operators	172
7.3.1	Fixed-length vectors of symbols	173
7.3.2	Permutations	174
7.3.3	Finite state machines	176
7.3.4	Symbolic expressions	177
7.4	Selection	179

7.5 Initialization	181
7.6 Summary	183
VIII What Is the Shortest Way?	185
8 The Traveling Salesman Problem	189
8.1 In search of good variation operators	191
8.2 Incorporating local search methods	214
8.3 Other possibilities	217
8.3.1 Edge assembly crossover	217
8.3.2 Inver-over operator	220
8.4 Summary	223
IX Who Owns the Zebra?	225
9 Constraint-Handling Techniques	231
9.1 General considerations	232
9.1.1 Designing $eval_f$	234
9.1.2 Design of $eval_u$	236
9.1.3 Relationship between $eval_f$ and $eval_u$	237
9.1.4 Rejecting infeasible solutions	239
9.1.5 Repairing infeasible individuals	239
9.1.6 Replacing individuals by their repaired versions	240
9.1.7 Penalizing infeasible individuals	240
9.1.8 Maintaining a feasible population using special representations and variation operators	241
9.1.9 Using decoders	242
9.1.10 Separating individuals and constraints	243
9.1.11 Exploring boundaries between feasible and infeasible parts of the search space	243
9.1.12 Finding feasible solutions	244
9.2 Numerical optimization	245
9.2.1 Methods based on preserving the feasibility of solutions .	246
9.2.2 Methods based on penalty functions	249
9.2.3 Methods based on a search for feasible solutions	257
9.2.4 Methods based on decoders	264
9.2.5 Hybrid methods	266
9.3 Summary	268
X Can You Tune to the Problem?	271
10 Tuning the Algorithm to the Problem	277
10.1 Parameter control in evolutionary algorithms	277
10.2 Illustrating the case with an NLP	282
10.3 Taxonomy of control techniques	284
10.4 The possibilities for parameter control	288

10.4.1 Representation	288
10.4.2 Evaluation function	289
10.4.3 Mutation operators and their probabilities	290
10.4.4 Crossover operators and their probabilities	293
10.4.5 Parent selection	295
10.4.6 Population	295
10.5 Combining forms of parameter control	296
10.6 Summary	298
 XI Can You Mate in Two Moves?	303
 11 Time-Varying Environments and Noise	307
11.1 Life presents a dynamic landscape	307
11.2 The real world is noisy	317
11.2.1 Ensuring diversity	321
11.3 Modeling of ship trajectory	325
11.4 Summary	329
 XII Day of the Week of January 1st	335
 12 Neural Networks	339
12.1 Threshold neurons and linear discriminant functions	340
12.2 Back propagation for feed forward multilayer perceptrons	345
12.3 Training and testing	350
12.4 Recurrent networks and extended architectures	352
12.4.1 Standard recurrent network	352
12.4.2 Hopfield network	352
12.4.3 Boltzmann machine	354
12.4.4 Network of multiple interacting programs	354
12.5 Clustering with competitive networks	356
12.6 Using neural networks to solve the TSP	358
12.7 Evolving neural networks	360
12.8 Summary	361
 XIII What Was the Length of the Rope?	363
 13 Fuzzy Systems	367
13.1 Fuzzy sets	368
13.2 Fuzzy sets and probability measures	368
13.3 Fuzzy set operations	369
13.4 Fuzzy relationships	372
13.5 Designing a fuzzy controller	375
13.6 Fuzzy clustering	380
13.7 Fuzzy neural networks	382
13.8 A fuzzy TSP	385
13.9 Evolving fuzzy systems	387

13.10 Summary	388
XIV Everything Depends on Something Else	389
14 Coevolutionary Systems	397
14.1 Playing a game	399
14.2 Learning to play checkers	400
14.3 Optimization through competing populations	403
14.4 Another example with a game	408
14.5 Artificial life	411
14.6 Games of cooperation and competition	412
14.7 Modeling intelligent agents	418
14.8 Issues in coevolution	420
14.9 An example of cooperative coevolution on the TSP	424
14.10 Summary	430
XV Who's Taller?	431
15 Multicriteria Decision-Making	435
15.1 Single numeric approach	440
15.1.1 The Valuated State Space approach	443
15.1.2 Fuzzy multicriteria decision-making	449
15.1.3 Summary	450
15.2 Evolutionary multiobjective optimization approach	451
15.2.1 Brief history	452
15.2.2 Evolutionary algorithm for multiobjective NLP	458
15.3 Summary	462
XVI Do You Like Simple Solutions?	465
16 Hybrid Systems	471
16.1 Summary	480
17 Summary	483
Appendix A: Probability and Statistics	495
A.1 Basic concepts of probability	495
A.2 Random variables	497
A.2.1 Discrete random variables	497
A.2.2 Continuous random variables	500
A.3 Descriptive statistics of random variables	502
A.4 Limit theorems and inequalities	505
A.5 Adding random variables	506
A.6 Generating random numbers on a computer	507
A.7 Estimation	508
A.8 Statistical hypothesis testing	511
A.9 Linear regression	512

XVIII Table of Contents

A.10 Summary	514
Appendix B: Problems and Projects	515
B.1 Trying some practical problems	517
B.2 Reporting computational experiments with heuristic methods . .	522
References	525
Index	551